



$$\begin{matrix} & \begin{matrix} A & B & C & D \end{matrix} \\ \begin{matrix} A \\ B \\ C \\ D \end{matrix} & \begin{pmatrix} \frac{1}{2} & \frac{1}{4} & 0 & \frac{1}{4} \\ \frac{1}{4} & \frac{1}{2} & \frac{1}{4} & 0 \\ 0 & \frac{1}{4} & \frac{1}{2} & \frac{1}{4} \\ \frac{1}{4} & 0 & \frac{1}{4} & \frac{1}{2} \end{pmatrix} \end{matrix}$$

$$M^2 = \begin{pmatrix} \frac{3}{8} & \frac{1}{4} & \frac{1}{8} & \frac{1}{4} \\ \frac{1}{4} & \frac{3}{8} & \frac{1}{4} & \frac{1}{8} \\ \frac{1}{8} & \frac{1}{4} & \frac{3}{8} & \frac{1}{4} \\ \frac{1}{4} & \frac{1}{8} & \frac{1}{4} & \frac{3}{8} \end{pmatrix}$$

$$M^3 = \begin{pmatrix} \frac{5}{16} & \frac{1}{4} & \frac{3}{16} & \frac{1}{4} \\ \frac{1}{4} & \frac{5}{16} & \frac{1}{4} & \frac{3}{16} \\ \frac{3}{16} & \frac{1}{4} & \frac{5}{16} & \frac{1}{4} \\ \frac{1}{4} & \frac{3}{16} & \frac{1}{4} & \frac{5}{16} \end{pmatrix}, \quad M^4 = \begin{pmatrix} \frac{9}{32} & \frac{1}{4} & \frac{7}{32} & \frac{1}{4} \\ \frac{1}{4} & \frac{9}{32} & \frac{1}{4} & \frac{7}{32} \\ \frac{7}{32} & \frac{1}{4} & \frac{9}{32} & \frac{1}{4} \\ \frac{1}{4} & \frac{7}{32} & \frac{1}{4} & \frac{9}{32} \end{pmatrix}$$

$$M^n = \begin{pmatrix} \frac{2^{n-1}+1}{2^{n+1}} & \frac{1}{4} & \frac{2^{n-1}-1}{2^{n+1}} & \frac{1}{4} \\ \frac{1}{4} & \frac{2^{n-1}+1}{2^{n+1}} & \frac{1}{4} & \frac{2^{n-1}-1}{2^{n+1}} \\ \frac{2^{n-1}-1}{2^{n+1}} & \frac{1}{4} & \frac{2^{n-1}+1}{2^{n+1}} & \frac{1}{4} \\ \frac{1}{4} & \frac{2^{n-1}-1}{2^{n+1}} & \frac{1}{4} & \frac{2^{n-1}+1}{2^{n+1}} \end{pmatrix}$$

can prove by induction...

$$4. \quad M^n \cdot \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} \frac{2^{n-1}+1}{2^{n+1}} \\ \frac{1}{4} \\ \frac{2^{n-1}-1}{2^{n+1}} \\ \frac{1}{4} \end{pmatrix} = \begin{pmatrix} P(A) \\ P(B) \\ P(C) \\ P(D) \end{pmatrix}$$

$$n \rightarrow \infty \quad \frac{2^{n-1} \pm 1}{2^{n+1}} = \frac{1}{4} \pm \frac{1}{2^{n+1}}$$

$$n \rightarrow \infty, \quad \frac{1}{2^{n+1}} \rightarrow 0$$

Probability each child holds parcel is $\frac{1}{4}$.