

Initial snowman:



1. If Frosty is half its height, its height will ~~going to~~ be $5R$.

$$\text{Decreased length: } 10R - 5R = 5R$$

$$\text{Decreased length for each snowballs: } 5R \div 2 = 2.5R$$

$$\text{Length of top snowball after melting: } 4R - 2.5R = 1.5R \text{ radius: } 0.75R$$

$$\text{Length of bottom snowball after melting: } 6R - 2.5R = 3.5R \text{ radius: } 1.75R$$

Volume ratio:

$$(0.75R)^3 \times \frac{4}{3}\pi + (1.75R)^3 \times \frac{4}{3}\pi : (2R)^3 \times \frac{4}{3}\pi + (3R)^3 \times \frac{4}{3}\pi$$

$$= 5.78125 : 35$$

$$= \underline{\underline{37:224}}$$

2. If Frosty is one tenth of its height, its height will be R .

$$\text{Decreased length: } 10R - R = 9R$$

$$\text{Decreased length for each snowballs: } 9R \div 2 = 4.5R$$

$$\text{Length of top snowball after melting: } 4R - 4.5R = -0.5R?$$

So we have to use a different method.

Let's say the top snowball already melted, and bottom snowball occupy the height of R .

It means that length of $5R$ ^{are} decreased to each snowballs.

$$\text{Length of bottom snowball after melting: } R \text{ radius: } 0.5R$$

Volume ratio:

$$(0.5R)^3 \times \frac{4}{3}\pi : (2R)^3 \times \frac{4}{3}\pi + (3R)^3 \times \frac{4}{3}\pi$$

$$= 0.125 : 35$$

$$= \underline{\underline{1:280}}$$