

Sticks Number

Arrangement of rectangles

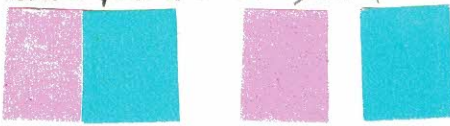
NO. of rectangles

1



1

2



3

3



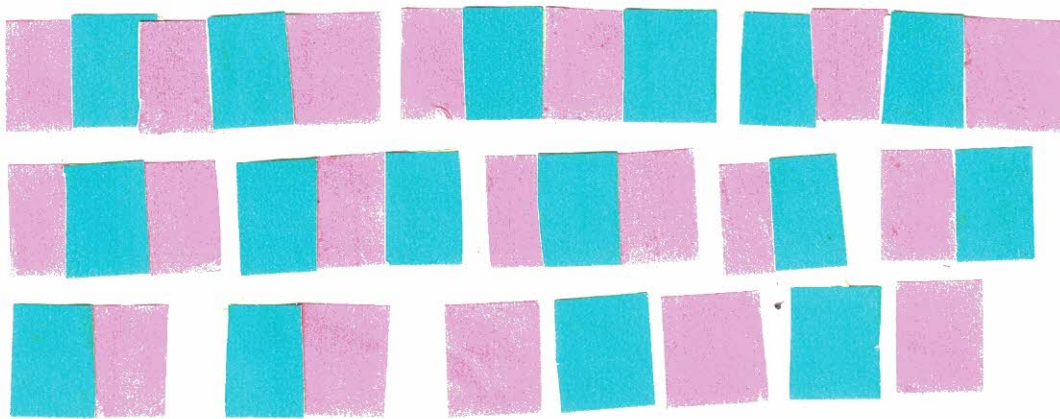
6

4



10

5

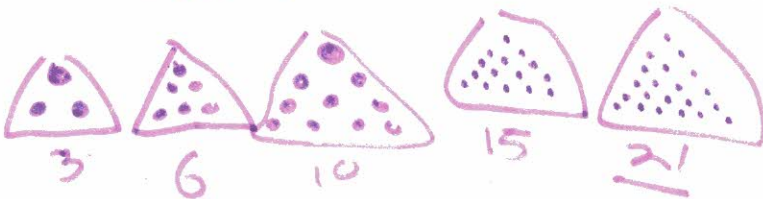


15

6

I predict that the next number is 21.

These numbers are all TRIANGULAR NUMBERS!



2  $1+2=3$   
 3  $1+2+3=6$   
 4  $1+2+3+4=10$   
 5  $1+2+3+4+5=15$   
 6  $1+2+3+4+5+6=21$

$1+2+3+4 \dots + (n-3) + (n-2) + (n-1) + n$

1	2	3	4
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$n$	$(n-1)$	$(n-2)$	$(n-3)$
$(n+1)$	$(n+1)$	$(n+1)$	$(n+1)$

There are  $n \div 2$  terms

The sum of the series is (triangle number)  
 equal to  $(n+1) \times (n \div 2)$

$$= (n+1) \times \frac{n}{2}$$

$n=100$  triangular no is  $(100+1) \times (\frac{100}{2})$

$n=1000$  triangular no is  $(1000+1) \times (\frac{1000}{2}) = 505000$

$$= 1001 \times 500 = 500500$$

Continue: explore further: squares

square types

Descriptions

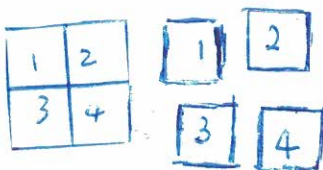
No. of squares

1 square



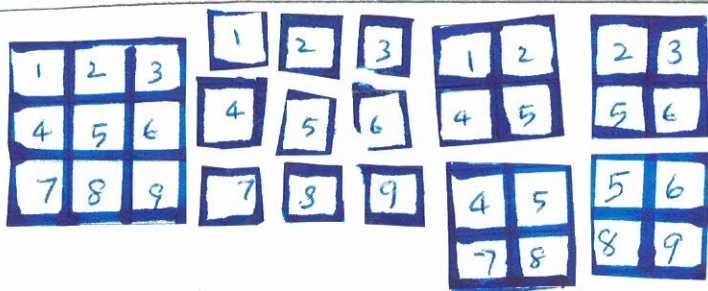
1

2x2 square



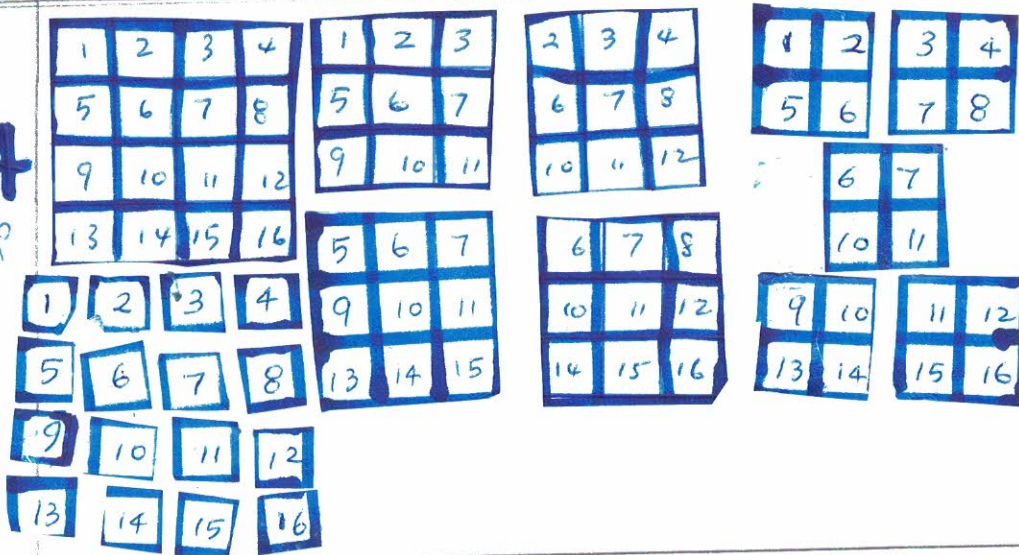
1+4

3x3 square



1+4+9

4x4 square



1+4+9+16

5x5 square

I predict 5x5 square has  $1+4+9+16+25$  squares

n x n square

There are  $1+2^2+3^2+4^2+5^2+\dots+n^2$  squares

Om Sri Hari Krishna, 100%

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